

Vector Wave Energy Migration (VWEM)

new approach to a universal migration method

[in Tesseral]

$$U_1(M, t) = \frac{1}{4\pi} \int_{\Sigma} \left\{ G \left[\frac{\partial u_1}{\partial n} \right] - [u_1] \frac{\partial G}{\partial n} + G \left[\frac{\partial u_1}{\partial t} \right] \frac{\partial \tau}{\partial n} \right\} d\Sigma + \frac{1}{4\pi} \int_V [u_1] \nabla^2 G dV$$

**Kirchhoff-Sobolev
Diffraction Integral**

Where:

G – Green function, which respond to wave equation;

τ – time function, which respond to the equation;

t – time;

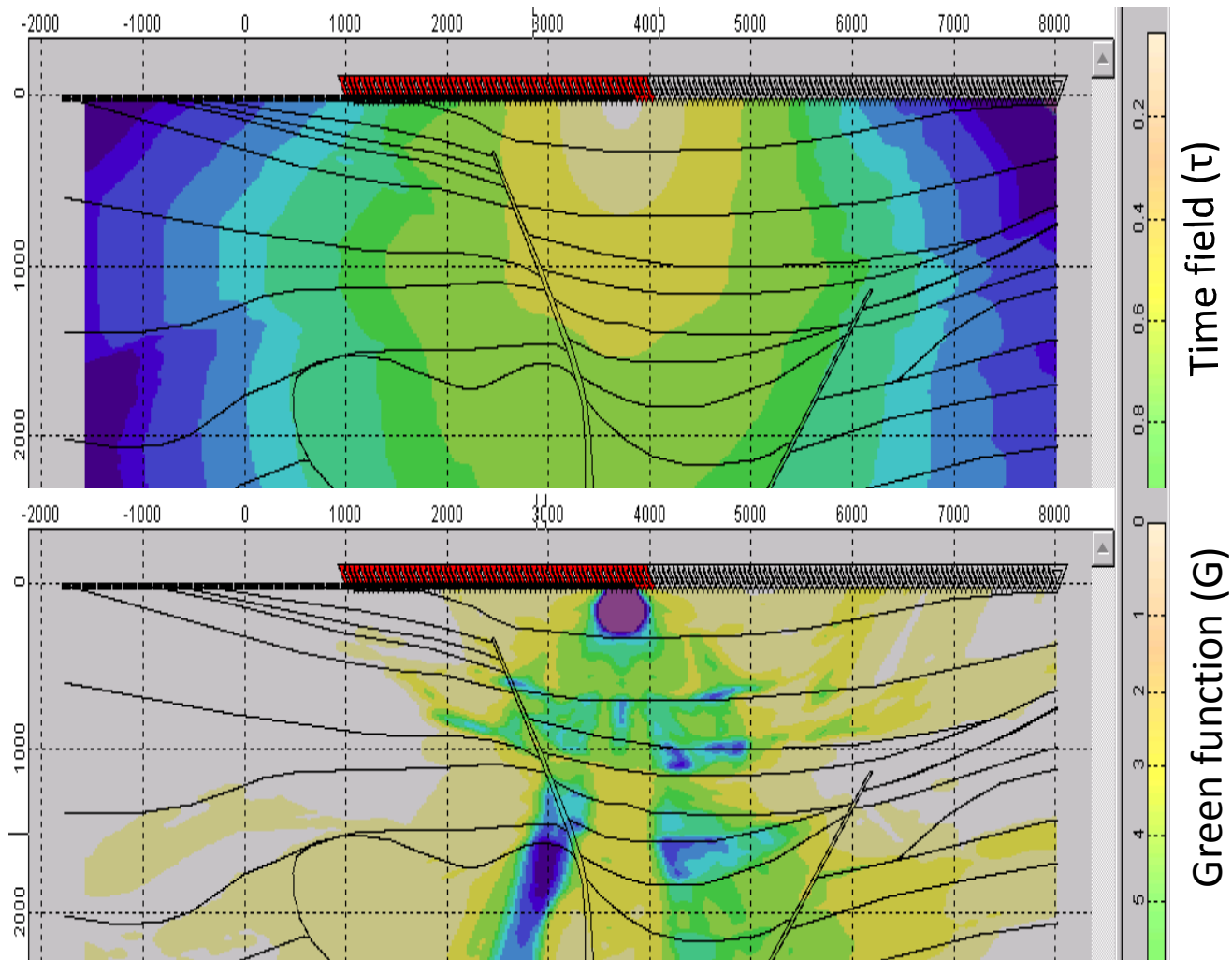
n – normal to the integration surface Σ .

U_1 - wave field component



www.tesseral-geo.com

Example of calculation of a time field and Green function



New capabilities of migration procedures

Hybrid algorithm of Kirchhoff migration based on vector wave equation (VWEM)

Not only P-wave migration operator tunings

First arrival

Maximum energy

Maximum divergence

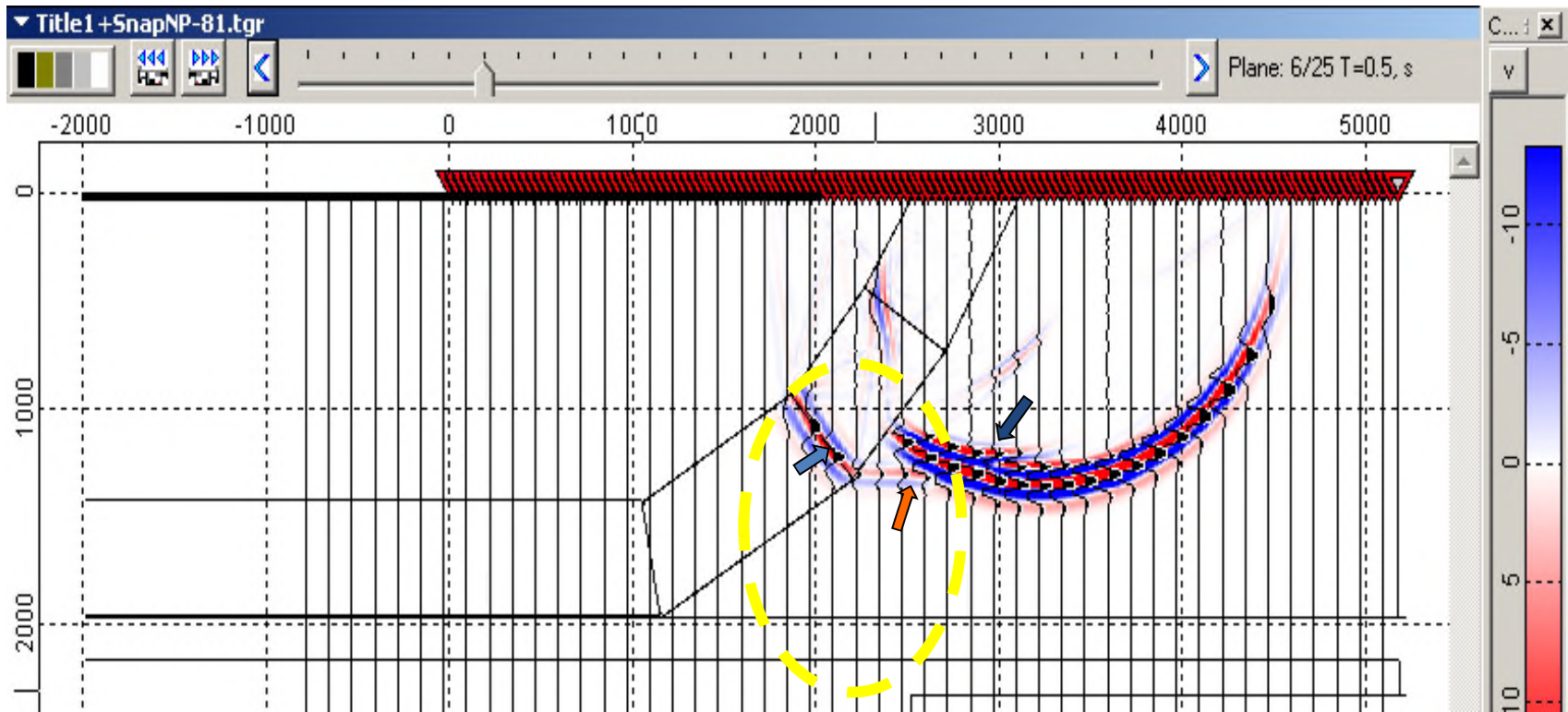
Maximum rotor

Maximum vertical component .. etc....

Macro \leftrightarrow micro model

Highly complex anisotropy

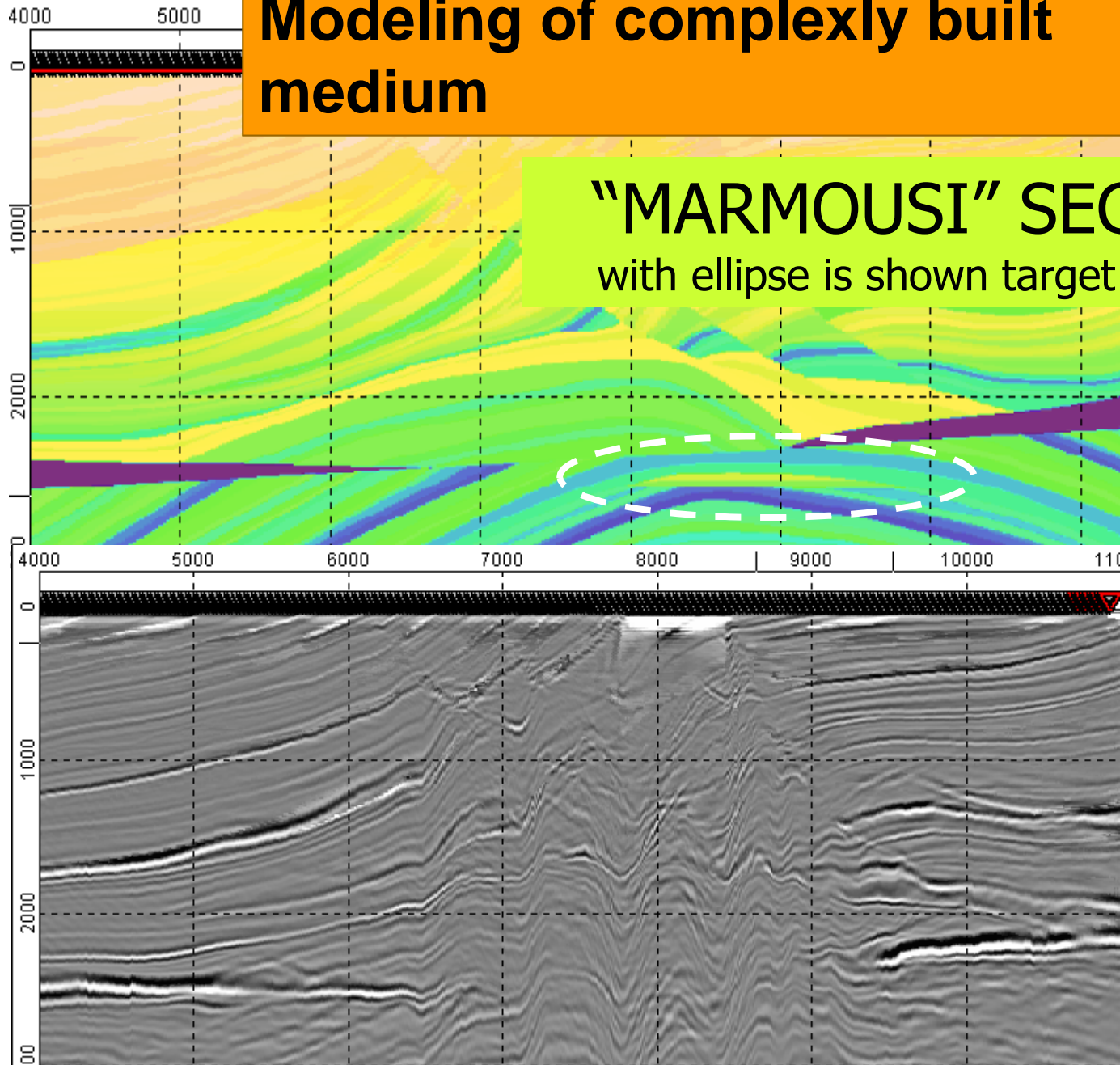
Maximum Energy vs First Arrival – multipath problem solutions



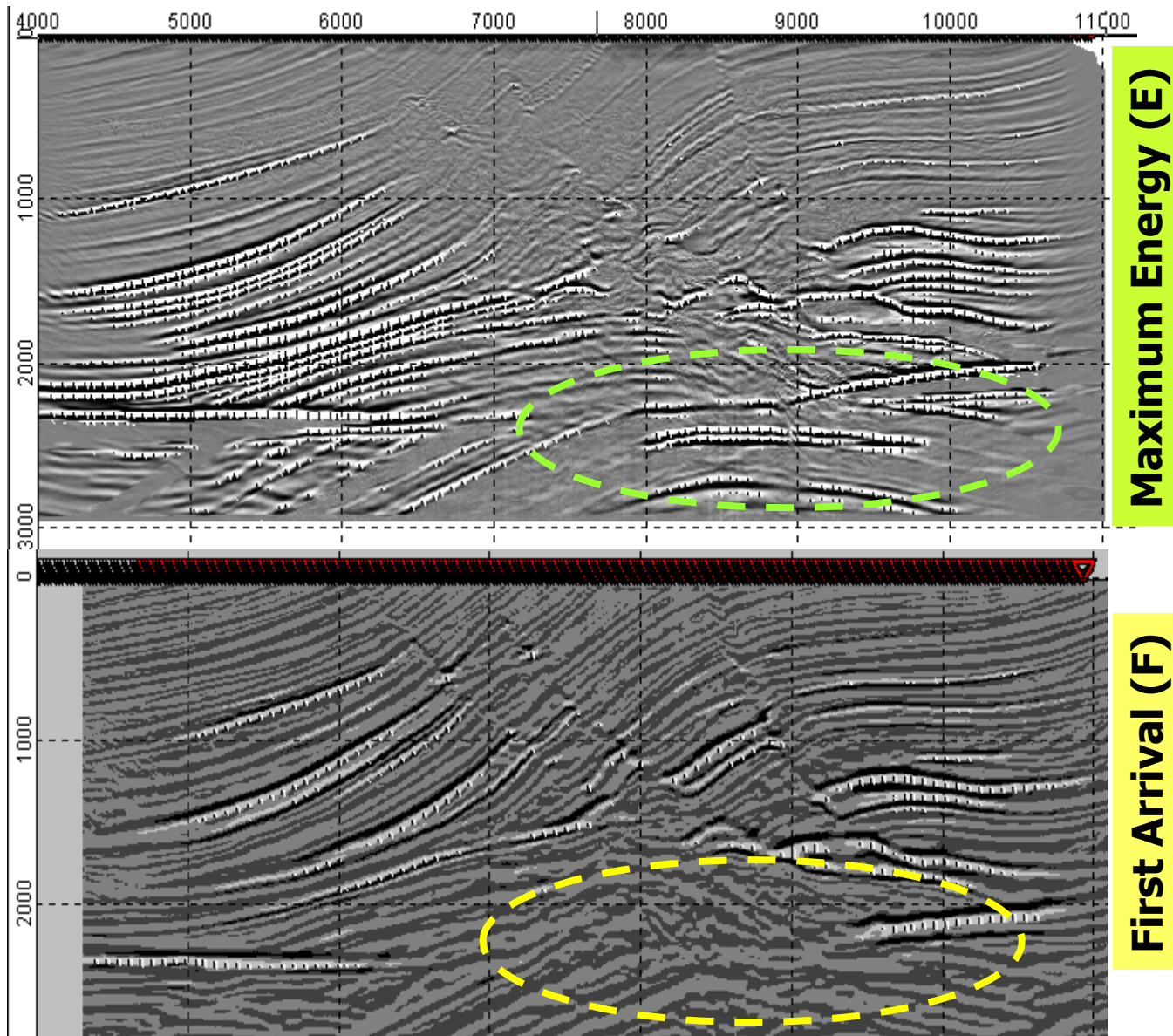
Example of ambiguity in determining time fields for pre-stack depth migration. In shadow area under high velocity crust wave with much lower energy (**red arrow**) is coming in first arrivals. High energy wave (**black arrow**) in this area is coming in later arrivals. If this wave is not taken into account **signal/noise ratio** at migration summation is very low.

Modeling of complexly built medium

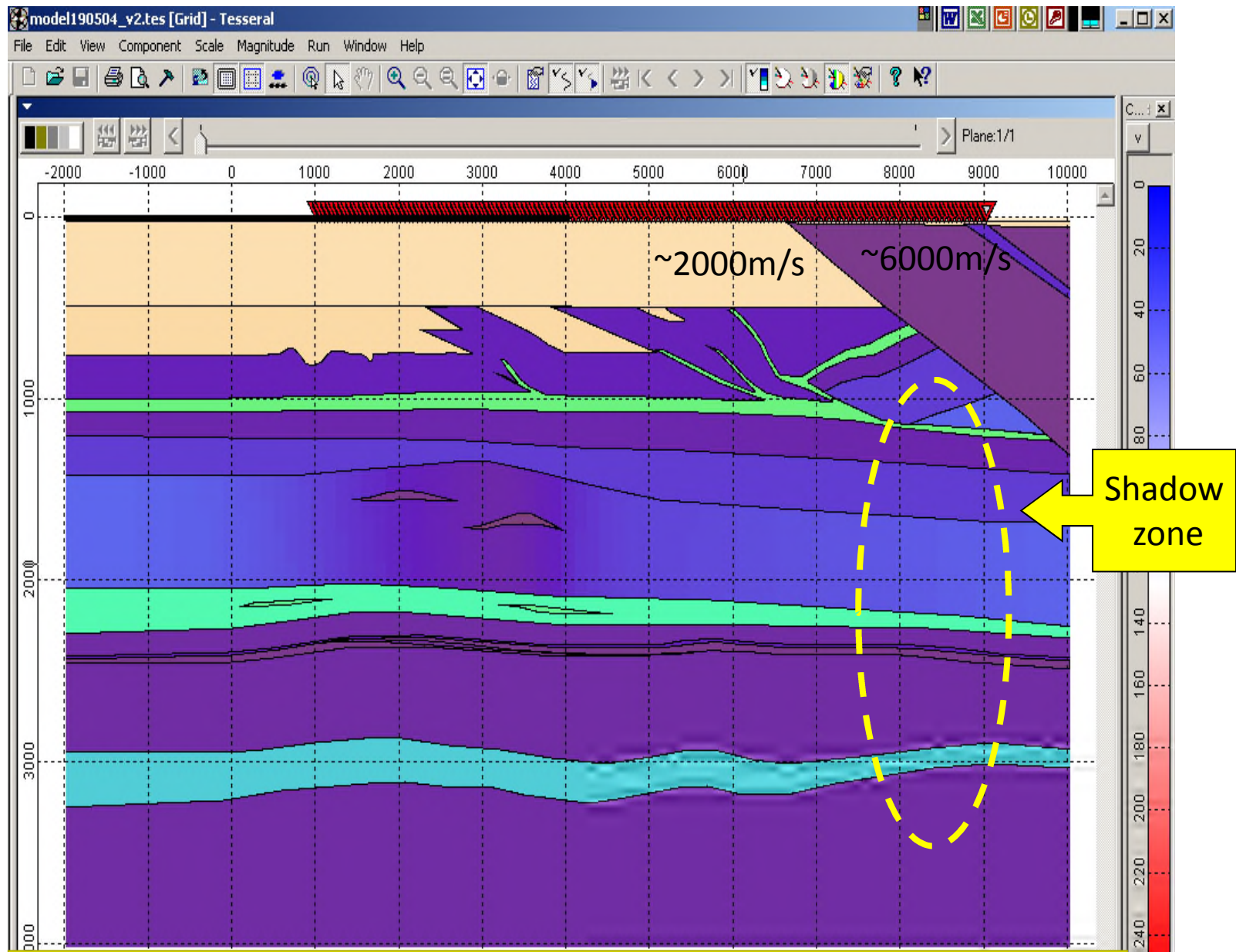
“MARMOUSI” SEG-Y-Model
with ellipse is shown target “gas deposit”



**Time Pre-stack
migration**



Migration procedures included in the package allow to check different processing sequence scenarios

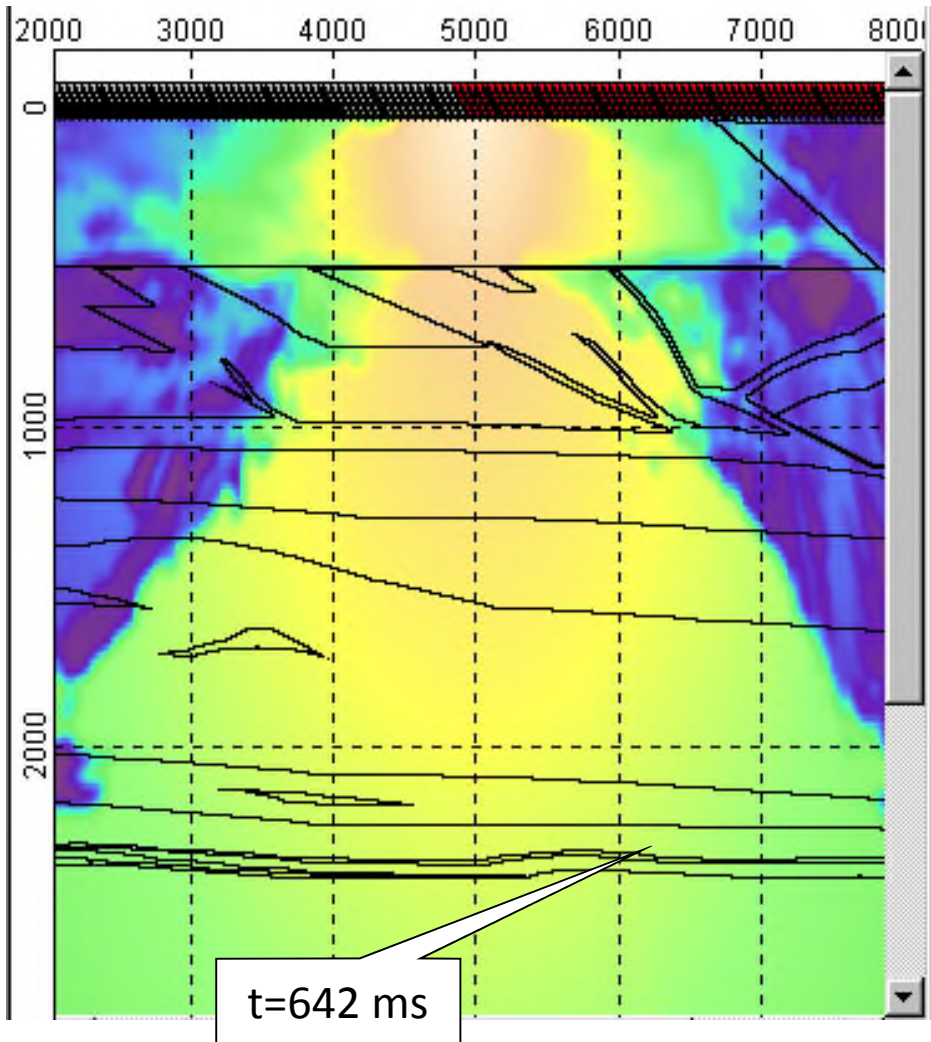


"Carbonate Trust" Velocity Model

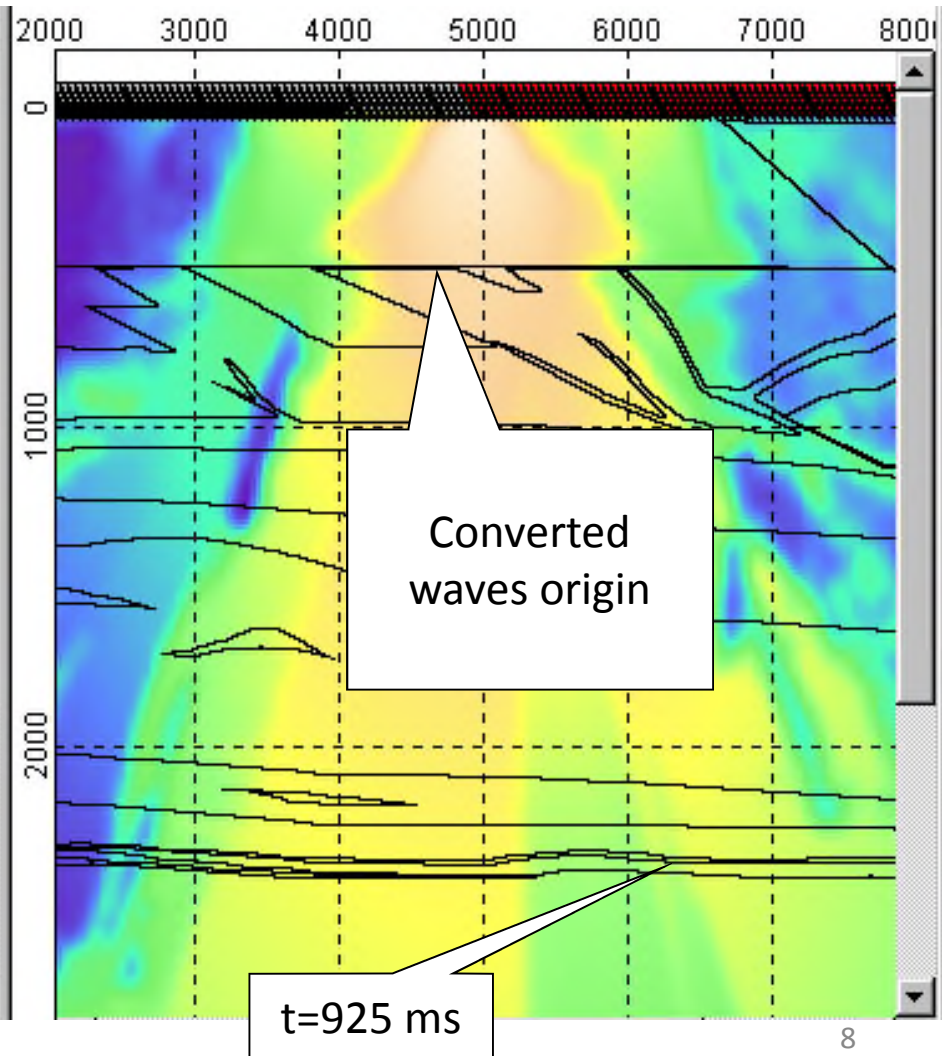
Incident wave timefields (*elastic wave equation*)

(Carbonate Trust) TIMEFIELDS: D^e -operator vs E^e -operator

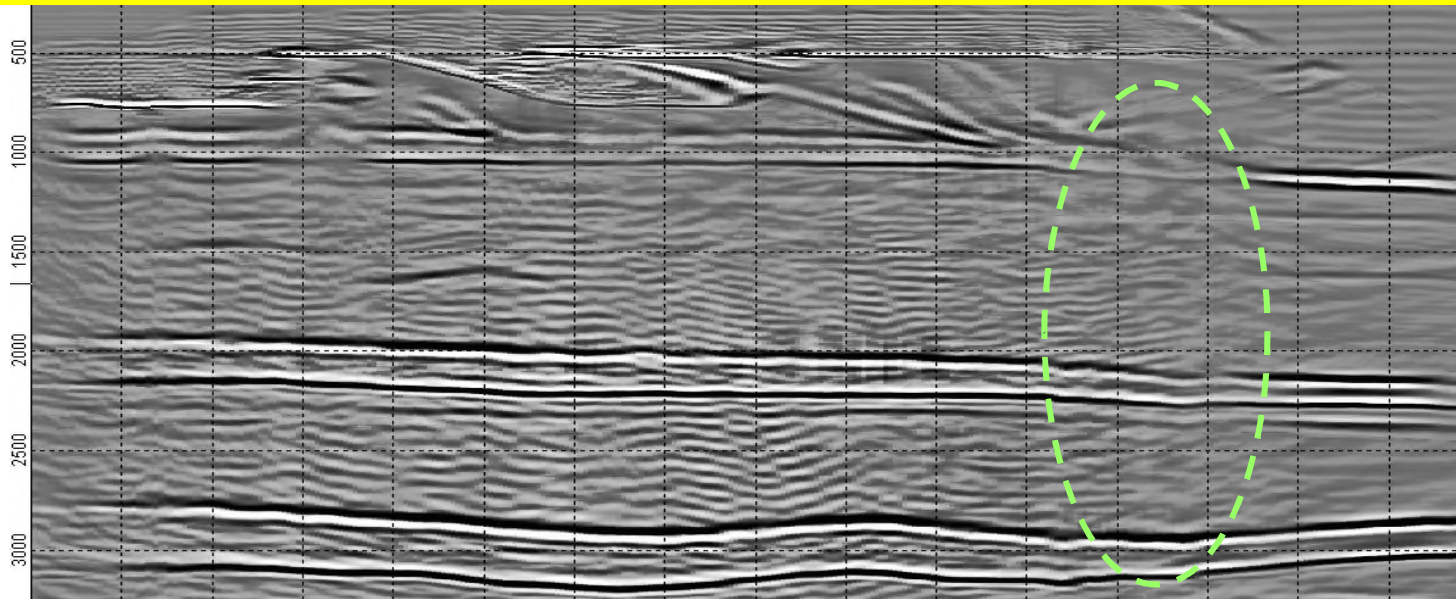
Maximum *Divergence* (D^e)



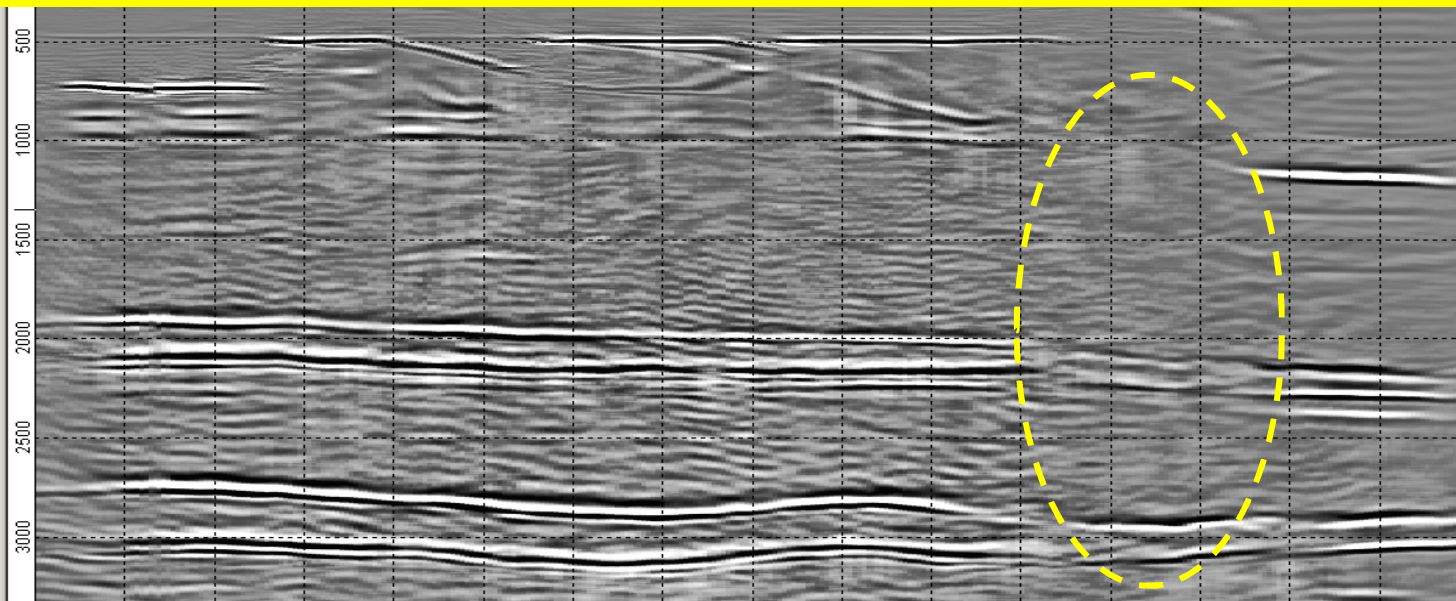
Maximum *Energy* (E^e)



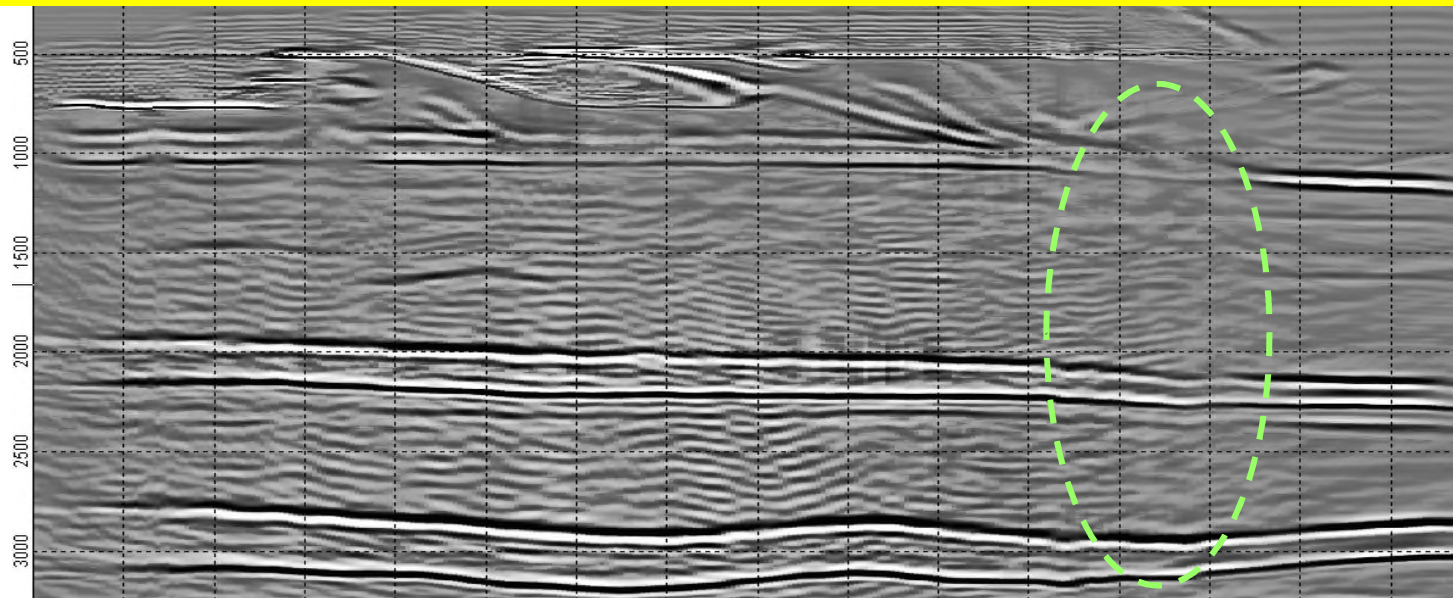
VWEM Maximum *Divergence elastic* wave equation (D^e)



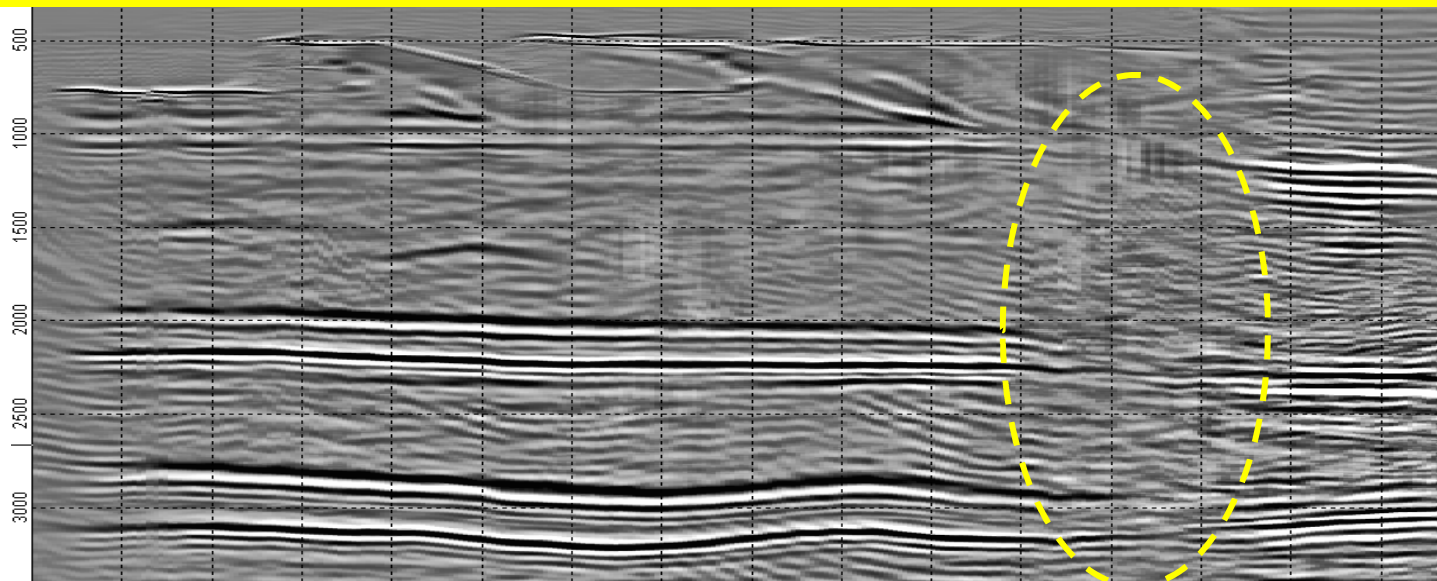
VWEM Maximum *Energy elastic* wave equation (E^e)



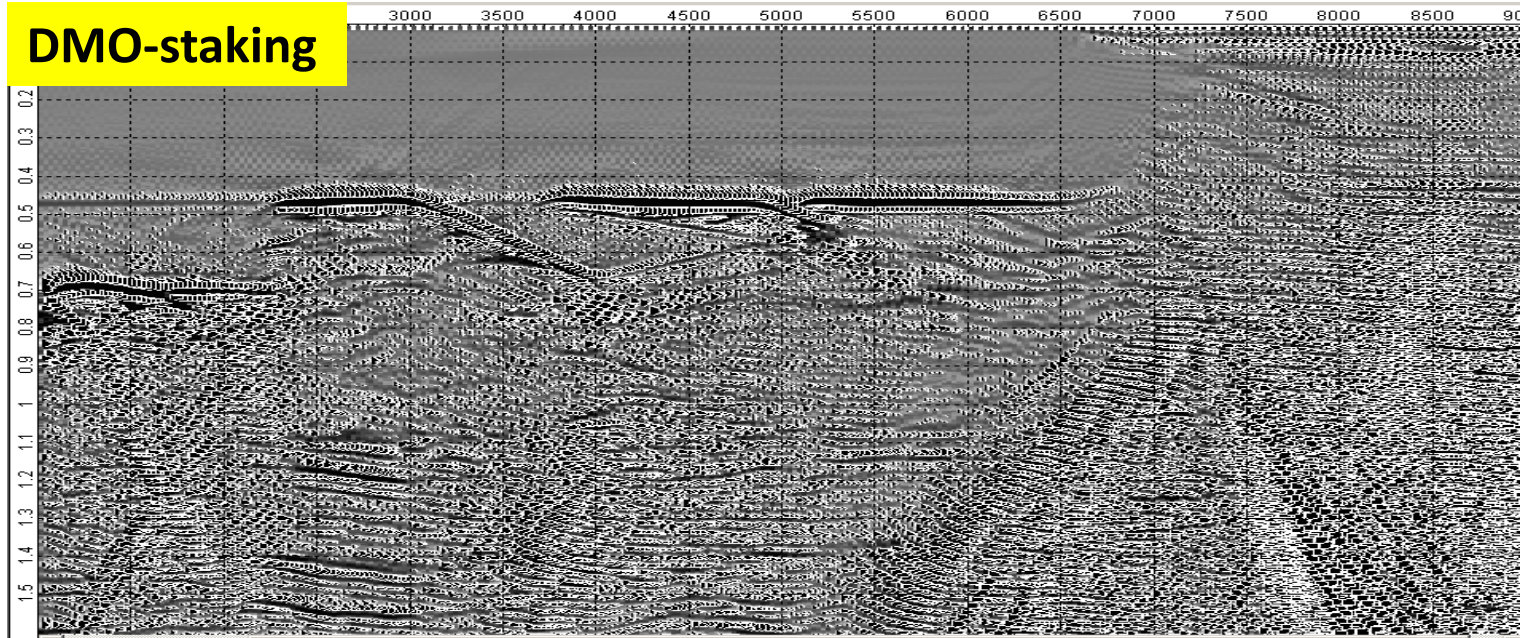
VWEM Maximum *Divergence elastic wave equation* (D^e)



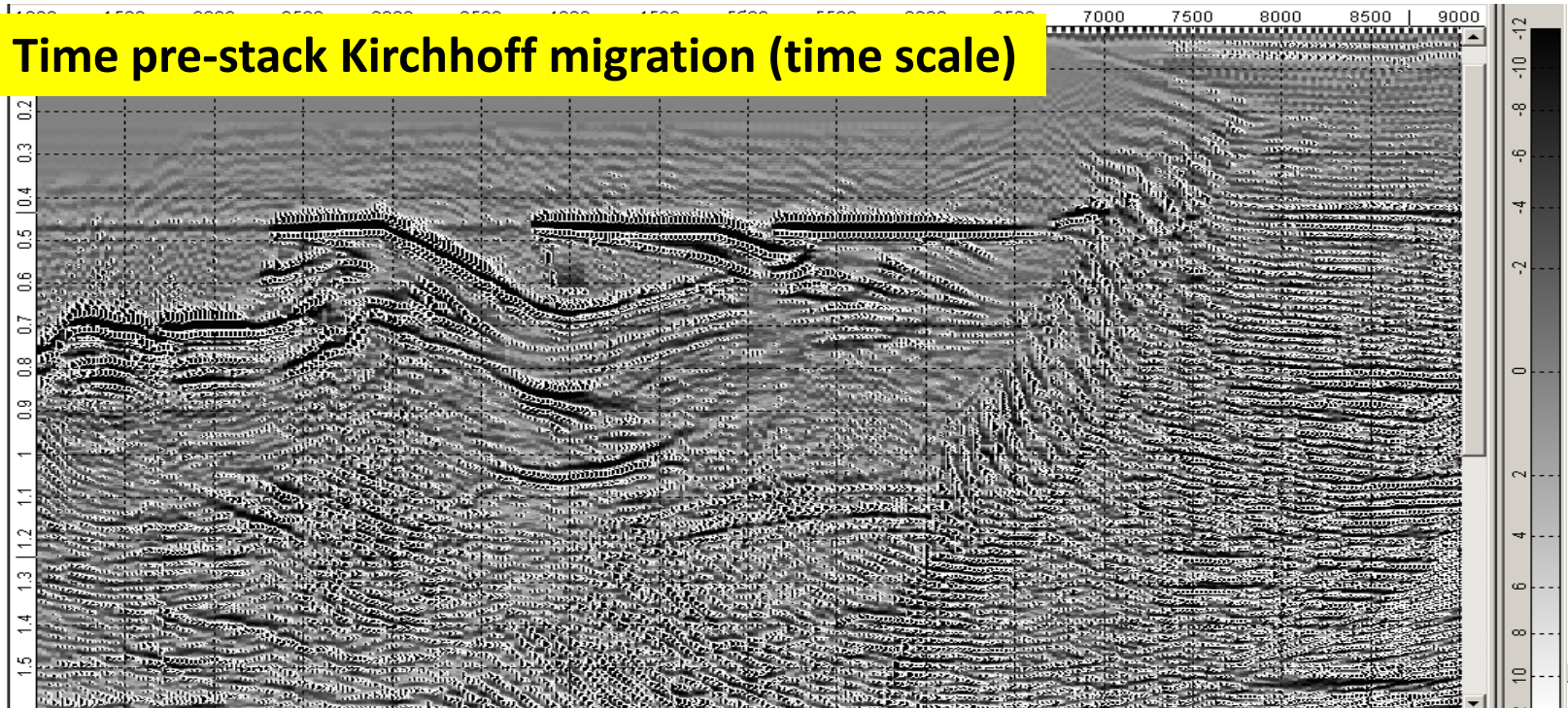
VWEM Maximum *Energy acoustic wave equation* (E^a)



DMO-staking

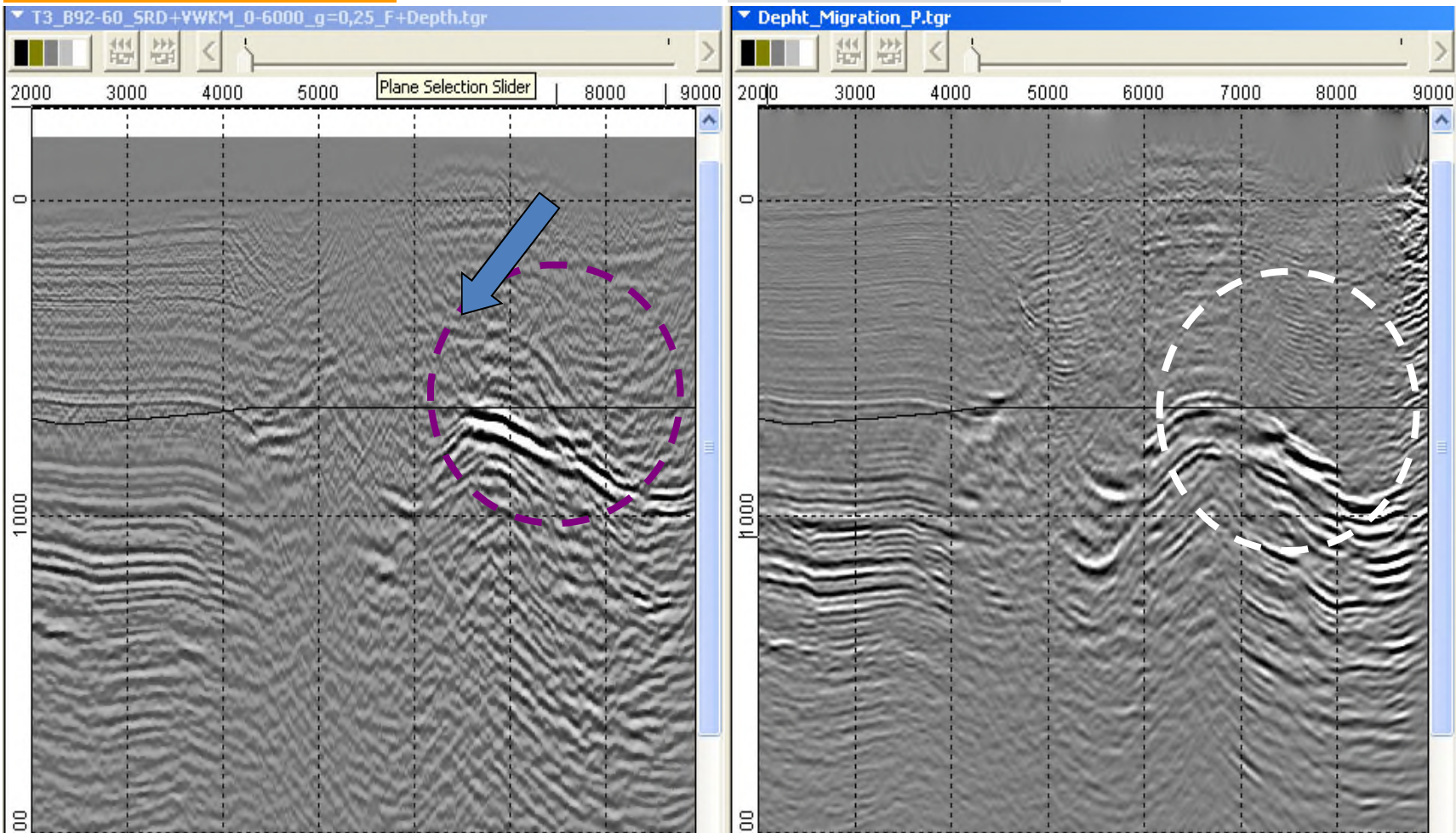


Time pre-stack Kirchhoff migration (time scale)



VWEM (D^E operator)

Wave PSDM



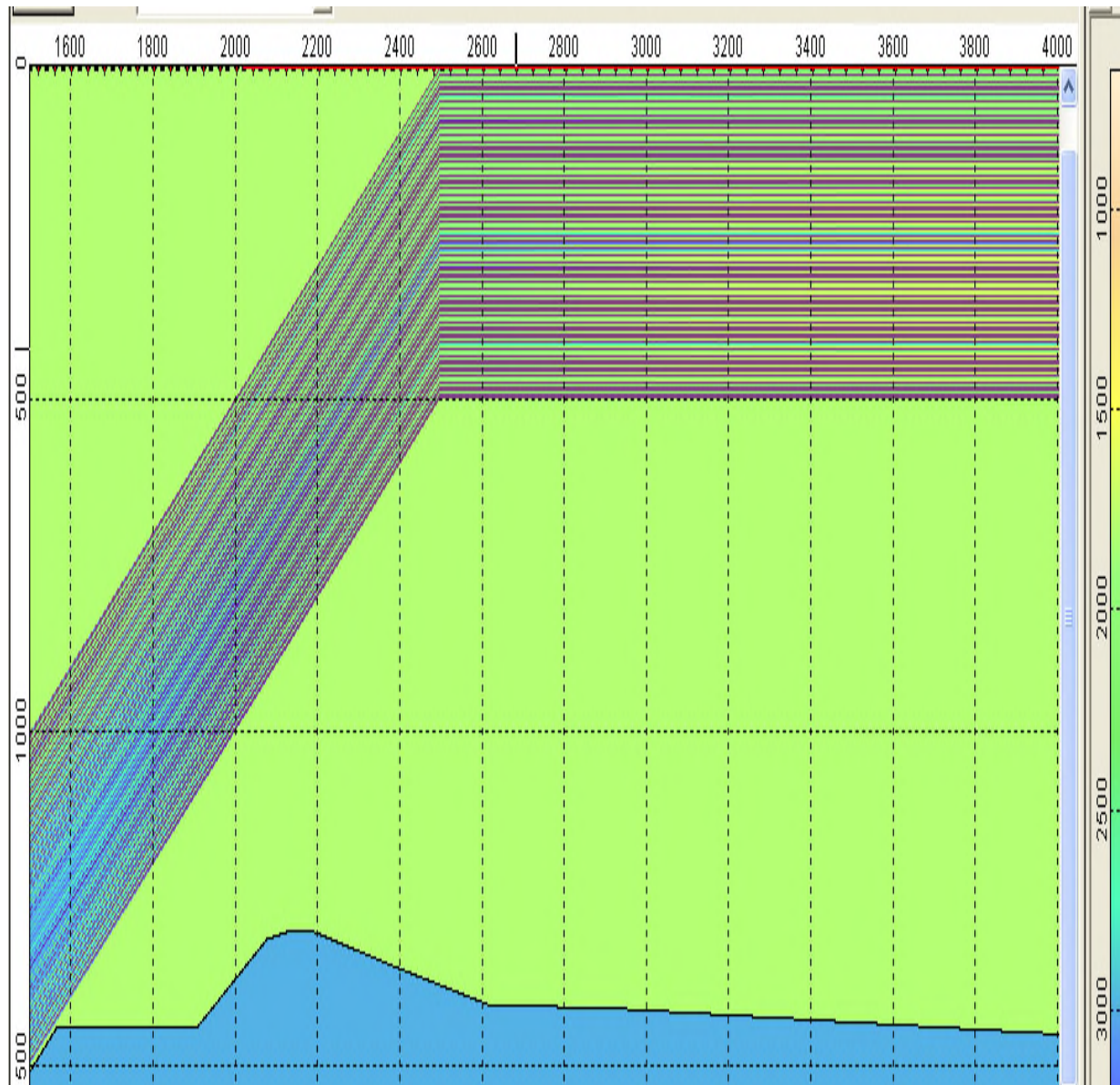
North Sea region on-shore profile.

Left: Seismic image is obtained with VWEM elastic maximum divergence (D^e) operator),

Right: PSDM based on scalar wave equation.

With arrow is shown area of considerable difference in imaging: presumably – pinnacle reef

“Where is the reef?” - thin layered variant



Parameters of the thin layers:

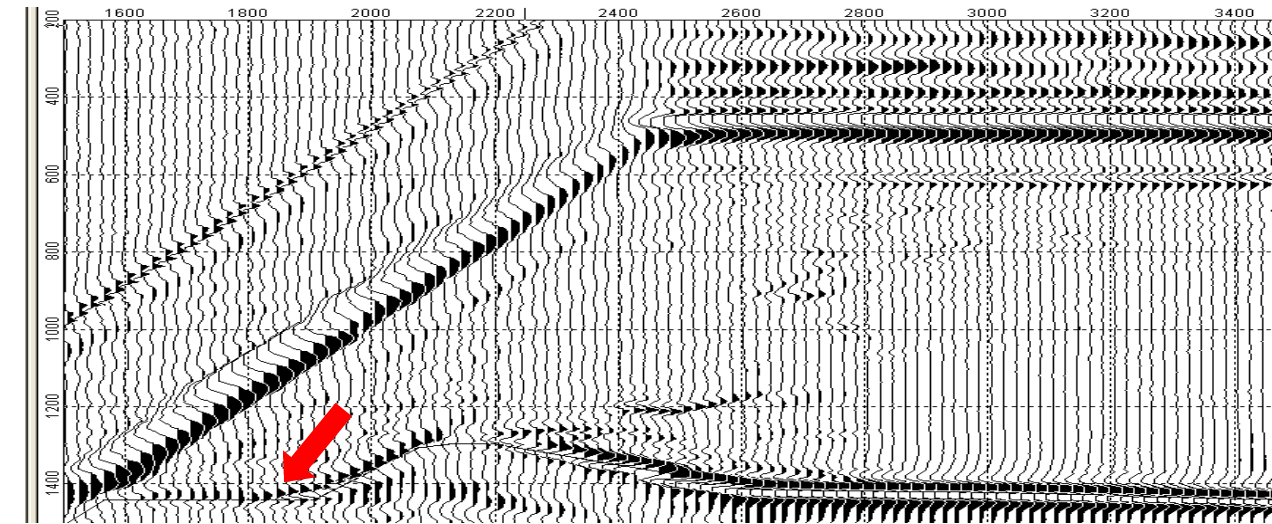
$$\Delta h = 10 \text{ m}, \lambda = 60 \text{ m}$$

$\alpha_1 = 4000 \text{ m/s}$, $\beta_1 = 2000 \text{ m/s}$,
 $\rho_1 = 2350 \text{ kg/m}^3$, $\alpha_2 = 2000 \text{ m/s}$,
 $\beta_2 = 1150 \text{ m/s}$, $\rho_2 = 2010 \text{ kg/m}^3$,
where α , β and ρ are P-wave,
S-wave velocities and
densities
in carbonates and shale,
respectively.

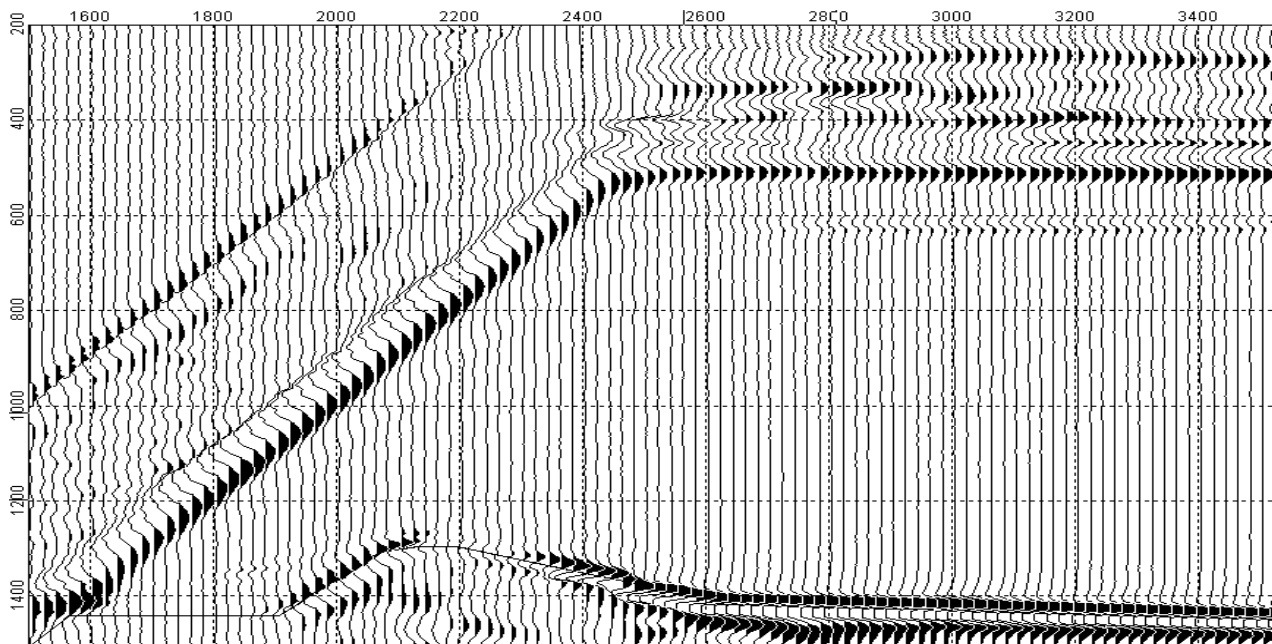
Backus's average parameters are follows:

$$\alpha_{\text{avg}} = 2470 \text{ m/s}, \beta_{\text{avg}} = 1450 \text{ m/s},$$
$$\epsilon = 0.32, \delta = 0.03.$$

Thin-layered «Where is the reef?» VWKM IMAGING (V^e -operator)



**VWKM: Maximum
Vertical Component
(*elastic* wave
equation)**



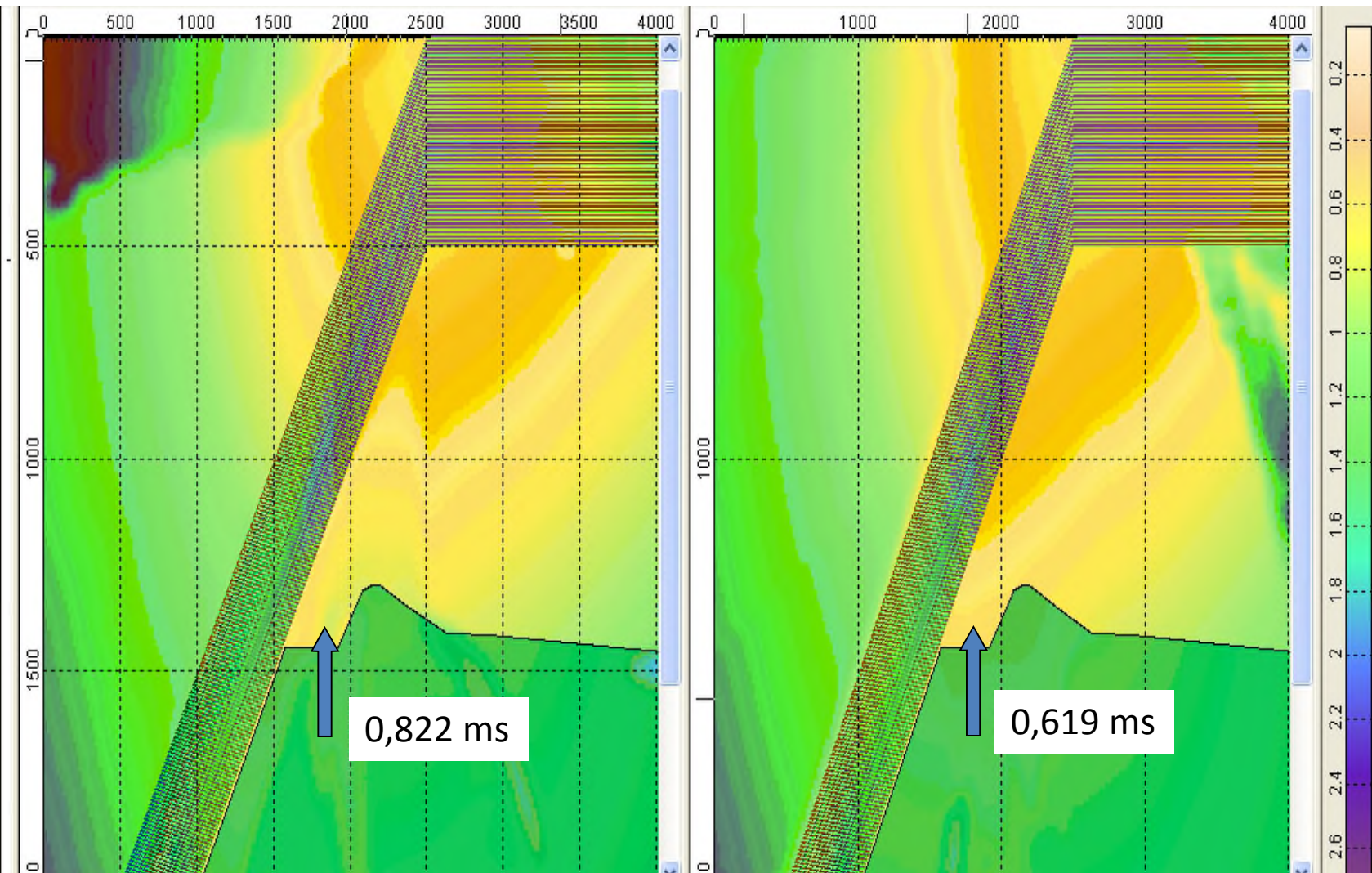
**VWKM: Maximum
Vertical Component
(*acoustic* wave
equation)**

Thin-layered «Where is the reef?»

Time Fields for Maximum *Vertical* Component

ELASTIC

ACOUSTIC

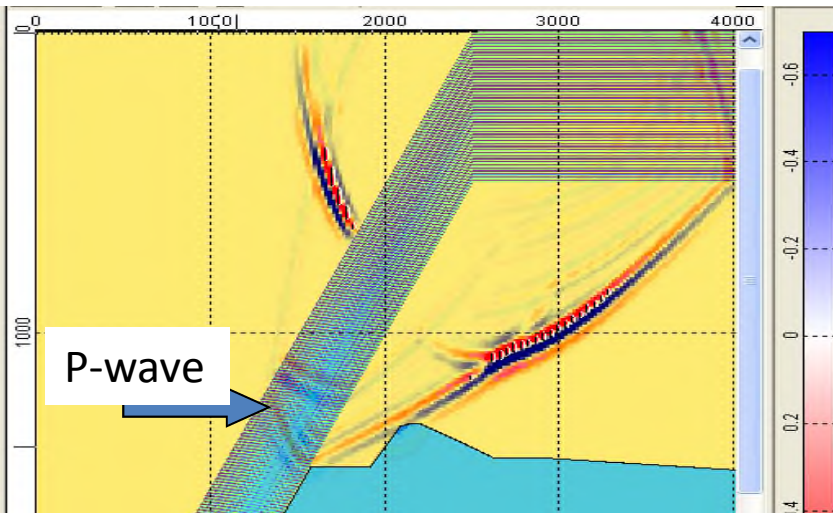
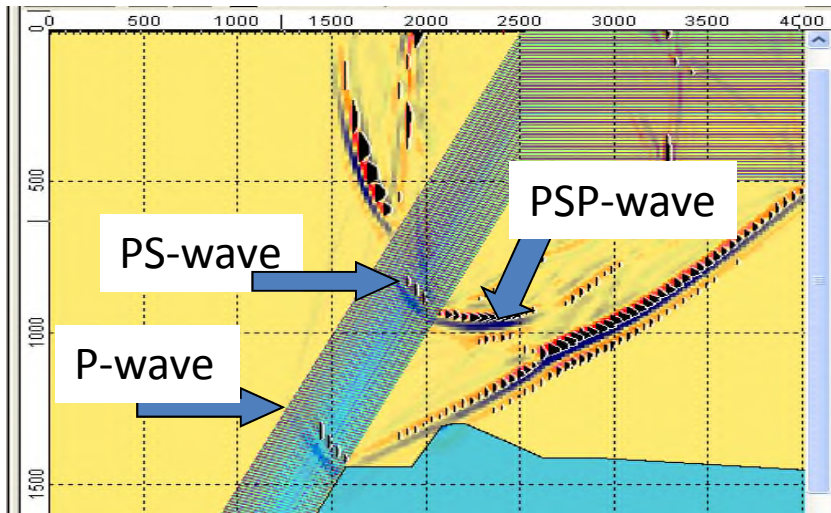


Thin-layered «Where is the reef?»

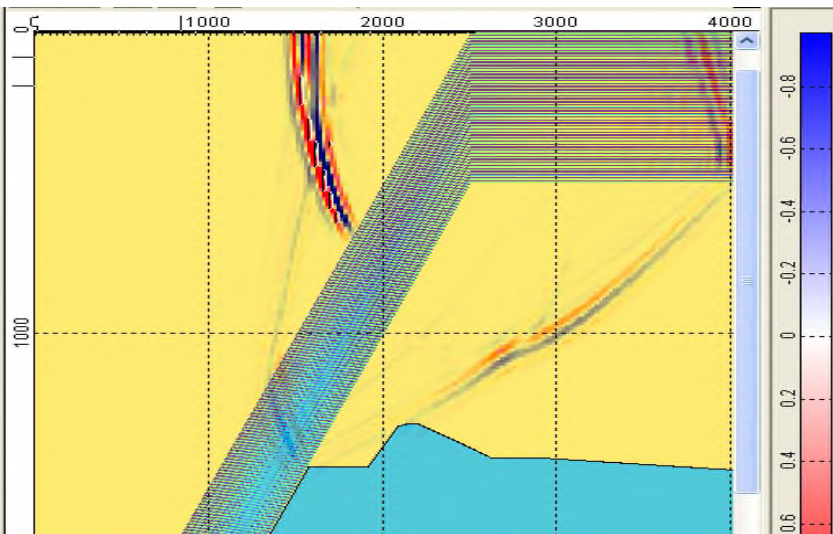
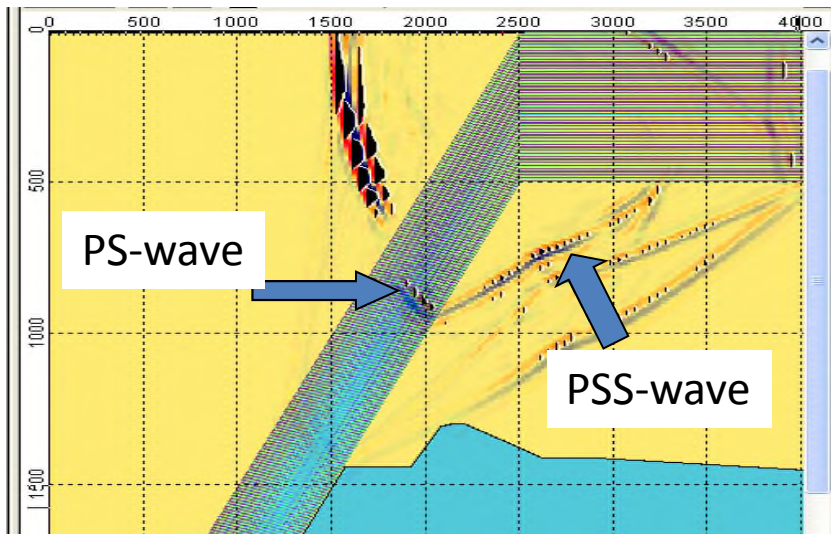
Snapshots of Elastic and Acoustic Waves

ELASTIC

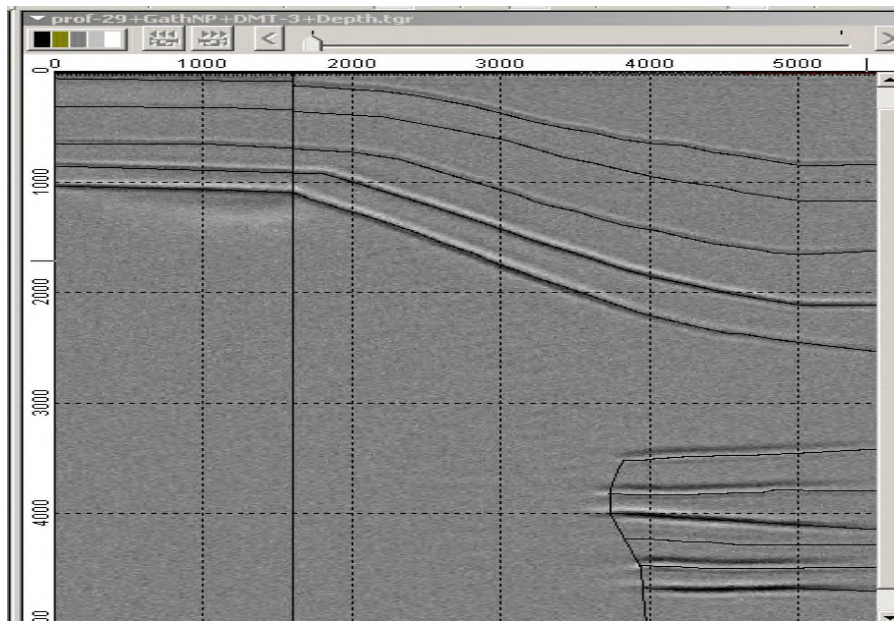
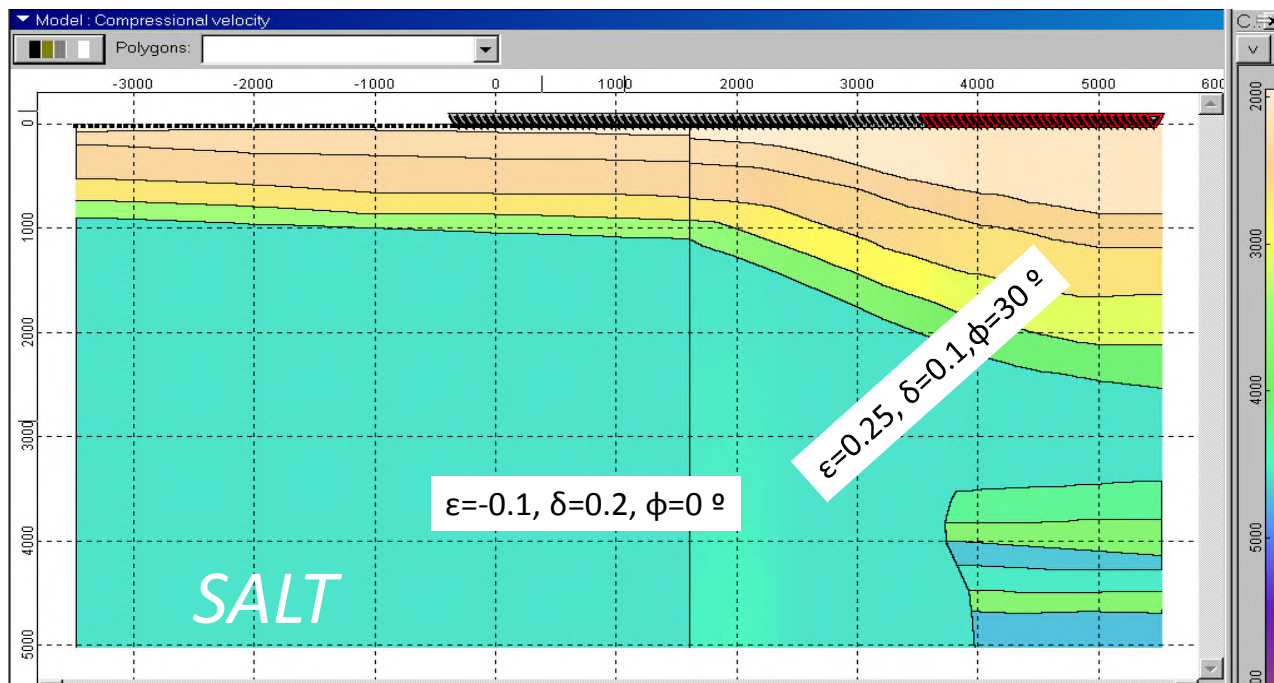
ACOUSTIC



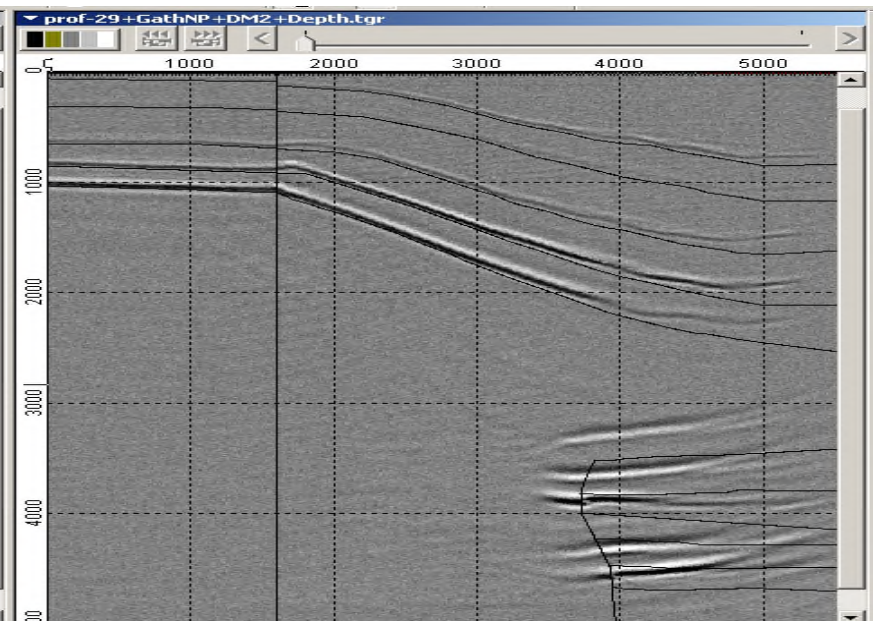
Snapshots of Z-component



Snapshots of X-component

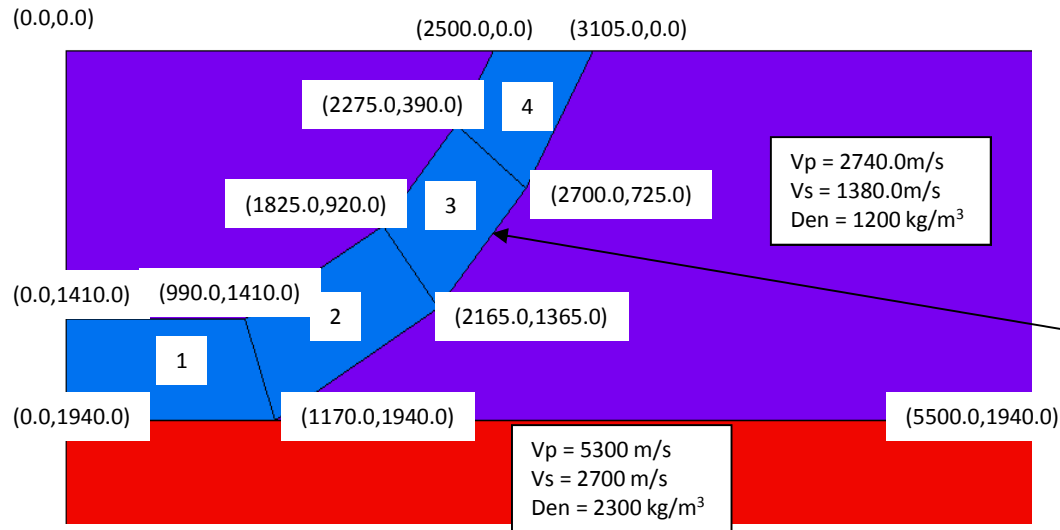


Taking anisotropy into account



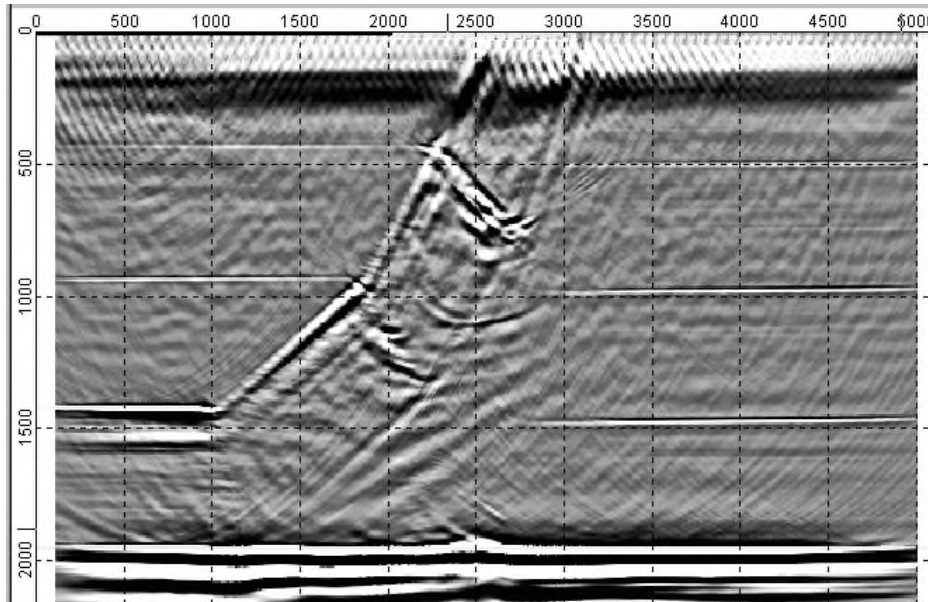
Not taking anisotropy into account

Physical model of anisotropic thrust by Lauton

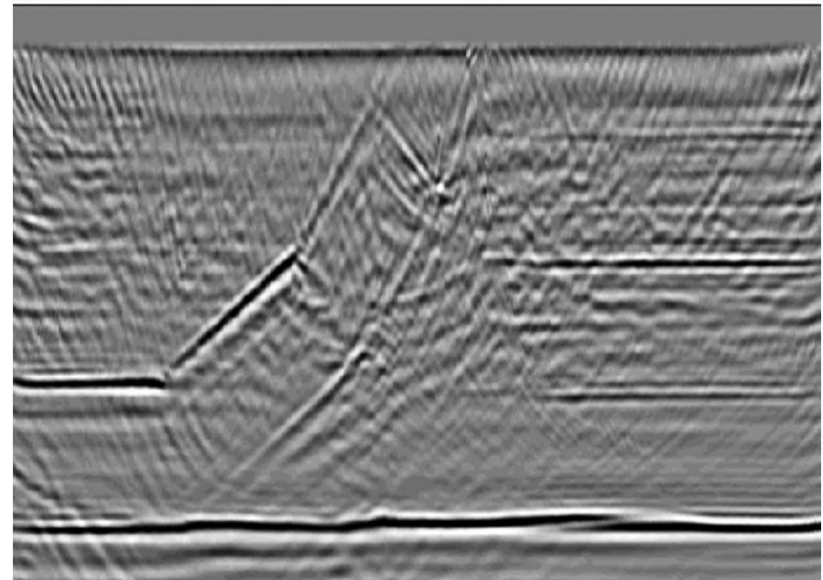


Anisotropic blocks: $V_{p0} = 2875 \text{ m/s}$; $V_{s0} = 1450 \text{ m/s}$; $\text{Den} = 1740 \text{ kg/m}^3$
 $\epsilon = 0.22$; $\delta = 0.10$

Dips: Block 1 = 0; Block 2 = 30.43; Block 3 = 49.67; Block 4 = 60.10



VWKM



PSDM (Veritas)

SUMMARY

Review of current challenges in migration processing

migration algorithms	Steep boundary angles	Strong lateral velocity variations	Topography	Rough seismic boundaries	Non-uniform shot point / receiver intervals	True amplitudes	Multipath operator	Solid Earth model (P/S/PS waves, true X,Z,Y component)	Highly complex anisotropy	Macro/micro model
VWEM	+	+	+	+	+	+	+	+	+	+
Two - Way Shot-Domain Prestack Imaging	+	+	+	-	-	+	-	-	-	-
One-Way Shot-Domain Prestack Imaging	-	+/-	-	-	-	+	-	-	+/-	-
One-Way Survey Sinking	-	+/-	-	-	-	+	+	-	+/-	-
Prestack Gaussian-beam depth migration	-	+	+	-	-	-	+	-	+/-	-

P017 ELASTIC MAXIMUM-ENERGY AND MAXIMUM-DIVERGENCE KIRCHHOFF MIGRATION

EAGE 67th Conference and Exhibition, Madrid, 2005.

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